Boyle's law shows that the pressure and volume of a gas are inversely related. Charles' law shows that the kelvin temperature and volume of a gas are directly related. These two relationships can be combined into a single equation known as the combined gas law. The formula for the combined gas law

is: $\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$ This equation could be memorized instead of memorizing Boyle's law, Charles' law, and

| 1 2 | | |
|------------------|---|-------------------|
| <u>Law</u> | Equation | Constant Variable |
| Boyle's Law | $\frac{P_1V_1}{X_k} = \frac{P_2V_2}{X_k}$ | temperature |
| Charles' Law | $\frac{R_1V_1}{T_1} = \frac{R_2V_2}{T_2}$ | pressure |
| Guy-Lussac's Law | $\frac{P_1 \mathbb{V}_1}{T_1} = \frac{P_2 \mathbb{V}_2}{T_2}$ | volume |

Guy-Lussac's law. Each of these other gas laws can be derived from the combined gas law by canceling out the variable that does not change.

USEFUL EQUATIONS

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \qquad T_K = T_C + 273$$

example

A 28 L sample of gas has a pressure of 25 psi when the temperature is 45°C. What is the volume of the gas if the pressure is increased to 175 psi and the temperature is increased to 320°C?

- list the variables:

$$V_I = 28 \text{ L}$$

$$P_1 = 25 \text{ psi}$$

$$V_1 = 28 \text{ L}$$
 $P_1 = 25 \text{ psi}$ $T_1 = 45^{\circ}\text{C} = 313 \text{ K}$ $V_2 = ?$ $P_2 = 175 \text{ psi}$ $T_2 = 320^{\circ}\text{C} = 593 \text{ K}$

- substitute into the equation:

$$\frac{P_1V_1}{T} = \frac{P_2V_1}{T}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \qquad \frac{(25 \text{ psi})(28 \text{ L})}{(313 \text{ K})} = \frac{(175 \text{ psi})(V_2)}{(593 \text{ K})}$$

- cross-multiply and simplify:

 $(25 \text{ psi})(28 \text{ L}) (593 \text{ K}) = (175 \text{ psi}) (V_2)(313 \text{ K})$

(25 psi)(28 L)(593 K) (175 psi)(V₂)(313 K) (175 psi) (313 K) (175 psi)(313 K)

- solve:

 $V_2 = 7.6 \, \text{L}$

Solve the following problems.

- 1. A canister containing air has a volume of 85 cm³ and a pressure of 1.45 atm when the temperature is 310 K. What is the pressure when the volume is increased to 180 cm³ and the temperature is reduced to 280 K?
- 2. Air is transferred from a 75 L tank where the pressure is 125 psi and the temperature is 288 K to a tire with a volume of 6.1 L and a pressure of 25 psi. What is the new temperature?
- 3. A helium balloon at 28°C has a volume of 1.8 L and a pressure of 102 kPa. What is the volume of the balloon when is rises into the atmosphere where the pressure is 85 kPa and the temperature is 4°C?
- 4. The pressure of a piston with a volume of 650 cm³ and 85°C is 830 torr. It is heated to 350°C and compressed to a volume of 65 cm³. What is the new pressure?
- 5. A gas tank has a volume of 28.1 m³ and a pressure of 18.4 atm. The temperature of the gas is 32°C. What is the Celsius temperature when the gas is put in an 11.2 m³ tank with a pressure of 22.7 atm?
- 6. A metal can is able to withstand 3800 kPa before is bursts. The gas in the can has a volume of 235 mL and the pressure is 110 kPa at 25°C. If the can is crushed to a volume of 8.5 mL and the temperature does not change will it burst? What is the pressure of the gas in the can?